

Erratum: Renormalization of the spin-wave spectrum in three-dimensional ferromagnets with dipolar interaction [Phys. Rev. B **74**, 014435 (2006)]

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The last term in Eq. (26) should read

$$\left(Dk^2 + \frac{S\omega_0}{2} \sin^2 \theta_{\mathbf{k}} \right) \left(\frac{S\omega_0^2 T}{2^7 D \sqrt{SD\omega_0}} + \frac{1}{\mathfrak{N}} \sum_{\mathbf{q}} \frac{|B_{\mathbf{q}}|^2}{S\epsilon_{\mathbf{q}}} (1 + 2N_{\mathbf{q}}) \right). \quad (1)$$

Equation (37) should read

$$\Omega(\omega, \mathbf{k}) = - (Dk^2)^2 \frac{2}{S} W(T) - Dk^2 \omega_0 \left(\sin^2 \theta_{\mathbf{k}} [W(T) + V(T)] - \frac{1}{2^7} \frac{T}{D} \sqrt{\frac{S\omega_0}{D}} \right) + \frac{S^2 \omega_0^3 T}{2^8 D \sqrt{SD\omega_0}} \sin^2 \theta_{\mathbf{k}}. \quad (2)$$

Thus, a new temperature-dependent term appears in Eqs. (26) and (37) originating from the term in Eq. (23) containing $Q_{\mathbf{q}}^{xx} - Q_{\mathbf{k}-\mathbf{q}}^{zz}$. In contrast, terms in Eqs. (26) and (37) containing demagnetizing factor \mathcal{N}_z have been discarded by the following reason. These terms stem from that in Eq. (23) containing $Q_{\mathbf{0}}^{zz} = \omega_0(\frac{1}{3} - \mathcal{N}_z)$. It can be shown using Eqs. (2), (7), (12), and (17) that this term leads to the following simple and quite natural renormalization of the bare value of the demagnetizing field $4\pi g\mu S\mathcal{N}_z$ [see Eq. (12)]: the spin value S in this expression is replaced by the spin value reduced by quantum and thermal fluctuations $\langle S_i^z \rangle = S - \langle a_i^\dagger a_i \rangle$ for which one has within the first order in $1/S$

$$\langle S_i^z \rangle = S - \frac{1}{\mathfrak{N}} \sum_{\mathbf{q}} \frac{E_{\mathbf{q}}(1 + 2N_{\mathbf{q}}) - \epsilon_{\mathbf{q}}}{2\epsilon_{\mathbf{q}}}. \quad (3)$$

Thus, $1/S$ corrections to $\Omega(\omega, \mathbf{k})$ containing \mathcal{N}_z do not contribute to renormalization of the spin-wave spectrum. Notice also that the spin-wave gap depends on T at $T \gg \sqrt{SD\omega_0}$.

I wish to emphasize that none of the final conclusions presented in my paper are affected by this change except for that about dependence of the spectrum on demagnetizing factor.